

# **Dynamics of CMEs in Interplanetary Space**

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**CDAW 2011: Do All CMEs Have Flux Rope Structure?**

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# INTRODUCTION

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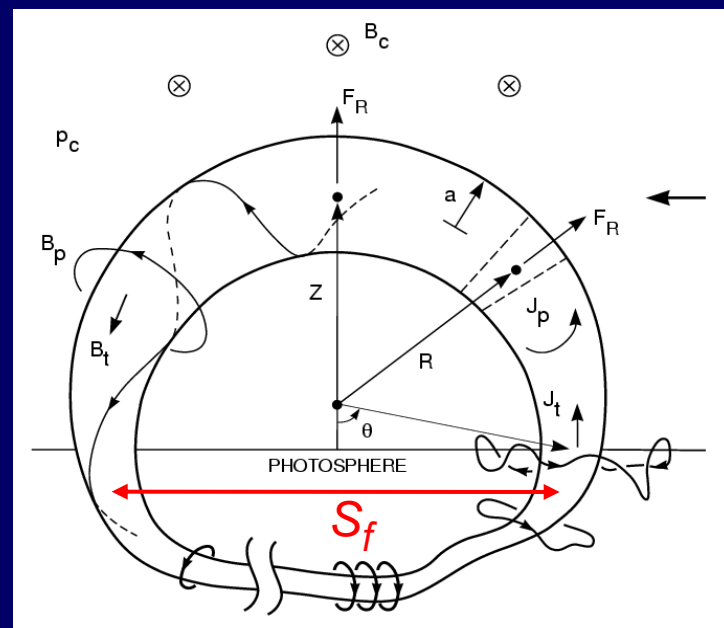
## LASCO observations

- Most CMEs can be interpreted as flux ropes (*Chen et al.* 1997)
- CME dynamics observed up to 30 Rs —→ Modeling limited to 2 – 30 Rs
- SECCHI observations – much wider field of view than LASCO
  - New challenges and opportunity to test the flux-rope hypothesis and our understanding of CME dynamics
- Magnetic clouds (MCs) defined by *Burlaga et al.* (1981) are the current channels of CME flux ropes (*Kunkel and Chen* 2010)
- This talk, analyse CME propagation from the Sun to 1 AU by using Flux Rope Model
  - Examine dynamics as a diagnostic of flux ropes: Characteristic magnetic forces
- I will focus on what determines the B field at 1 AU and show that
  - the CME height-data trajectory alone allows us to predict the B field at 1 AU and
  - the strength of B field and the CME arrival time at 1 AU depend on the amount of poloidal magnetic energy injected.

# FLUX ROPE GEOMETRY

## Initial Structure:

- Flux rope parameters: Specify  $Z$ ,  $S_f$ ,  $R/a$ 
  - Footpoint separation distance is fixed
  - $R$  = determined by  $Z$ ,  $S_f$
  - Set  $R_0/a_0 = 2$  (based on previous work)
- Pressure:  $p_a(Z)$  = outside flux rope (model),  $\bar{p}_0$  = inside (specified, usually  $p_a/2$ )
- $B_c$  = overlying coronal field (specified)
- Initial Equilibrium: forces are balanced
  - Electric currents:  $I_t$ ,  $I_p$  (calculated)
  - Magnetic field:  $B_p$ ,  $B_t$  (calculated)
  - Total mass:  $M_T$  (calculated)



# PHYSICS OF CMEs: Forces

- “Toroidal” magnetic flux rope *with fixed footpoints* separated by  $S_f$
- Major Radial Forces: integrate  $\mathbf{f} = \rho d\mathbf{v} / dt = c^{-1} \mathbf{J} \times \mathbf{B} - \nabla p + \rho \nabla \phi_g$

$$\rightarrow M \frac{d^2 Z}{dt^2} = \frac{\Phi_p^2(t)}{c^4 L^2 R} \left[ \ln \left( \frac{8R}{a} \right) + \frac{1}{2} \beta_p - \frac{1}{2} \frac{B_t^2}{B_p^2} + 2 \left( \frac{R}{a} \right) \frac{B_c}{B_p} - 1 + \frac{\xi_i}{2} \right] + F_g + F_d$$

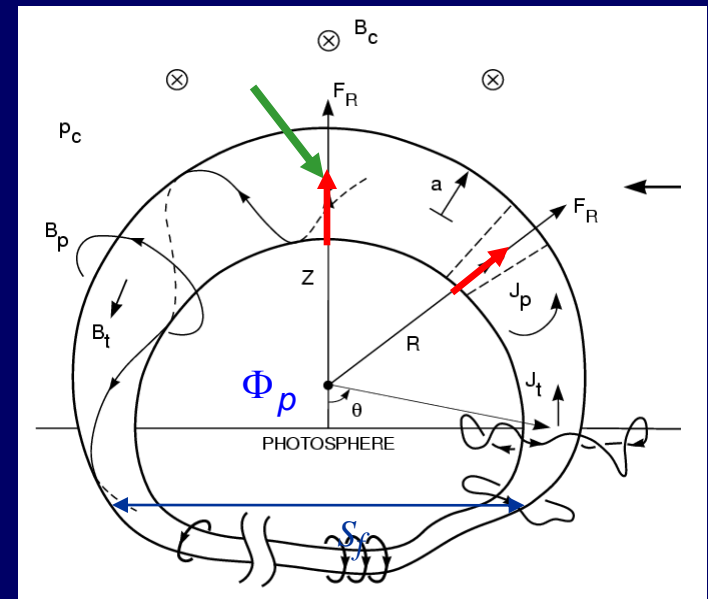
[Shafranov 1966; Chen 1989;  
Garren and Chen 1994]

$$\rightarrow M \frac{d^2 a}{dt^2} = \frac{a}{4} \left( B_t^2 - B_p^2 + \beta_p B_p^2 \right)$$

$$\Phi_p = c L I_t, \quad L = 4\pi \Theta R \left[ \ln \left( \frac{8R}{a_f} \right) - 2 \right]$$

- Initiation of eruption:

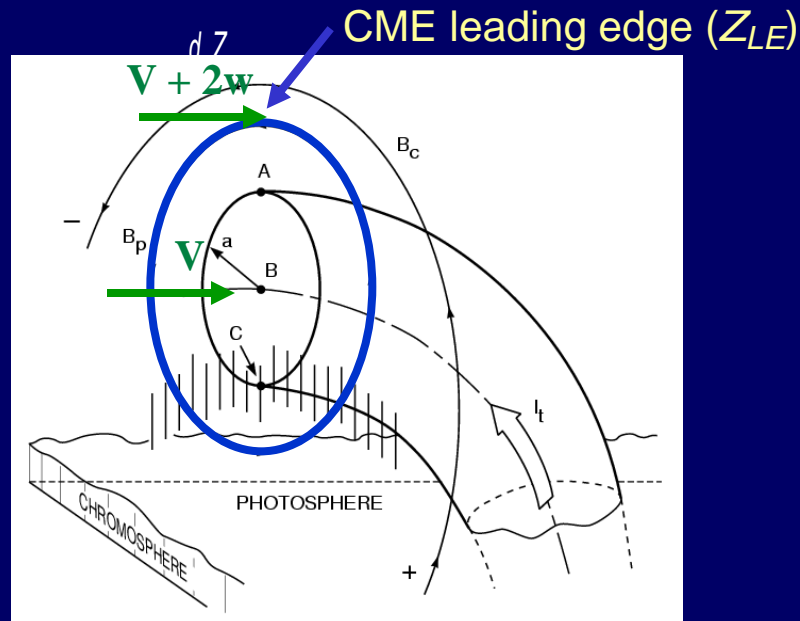
$$\frac{d\Phi_p(t)}{dt} = \text{poloidal flux "injection"}$$



# DRAG FORCE

- Use drag force to account for momentum coupling between the flux rope and the ambient plasma
- Drag force: the expanding flux rope displaces the surrounding plasma, transferring momentum

$$F_d = 2C_d a \rho_{sw} [V_{sw} - (V + 2w)] |V_{sw} - (V + 2w)|$$



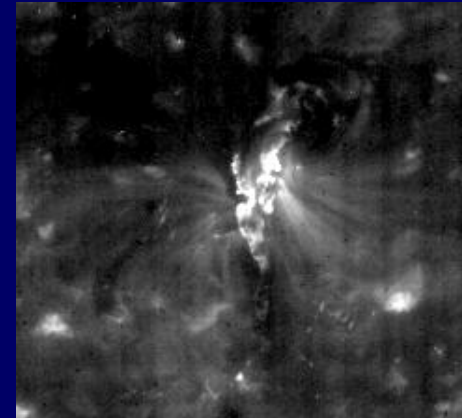
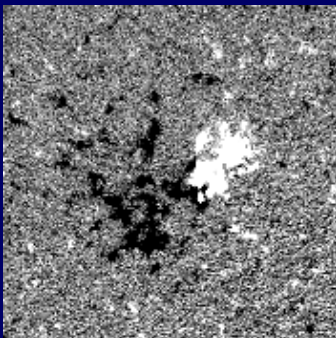
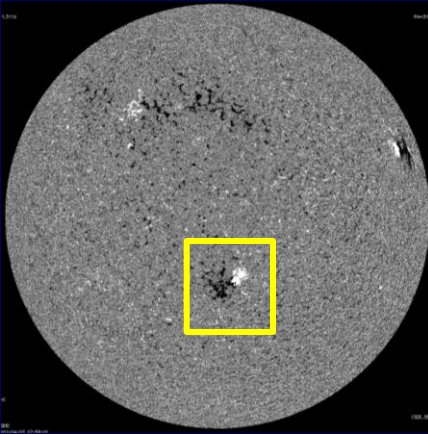
Chen (JGR, 1996)

# CONSTRAINTS ON INITIAL CONDITIONS

- Initial Flux Rope (3 April 2010) source region is identified
  - Use EUVI and MDI data to determine footpoints ( $S_f$ ), height ( $Z_0$ )

- Footpoints

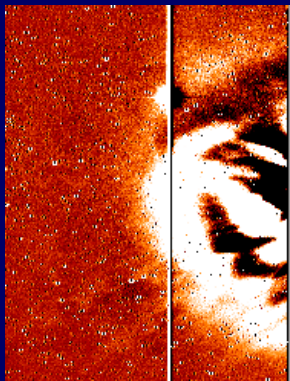
- $S_f = 1.0 \cdot 10^{10}$  cm
- $Z_0 = 3.1 \cdot 10^9$  cm
- Aspect ratio = 2



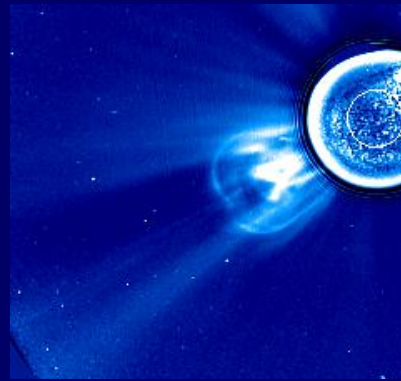
# HEIGHT-TIME MEASUREMENT

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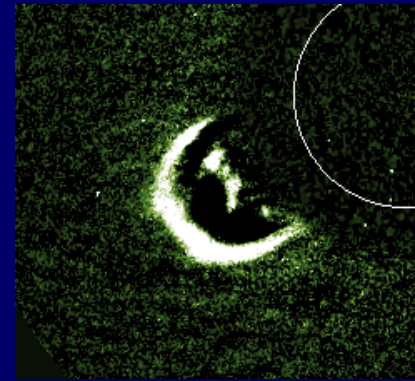
Track leading-edge height



Stereo A , HI 1

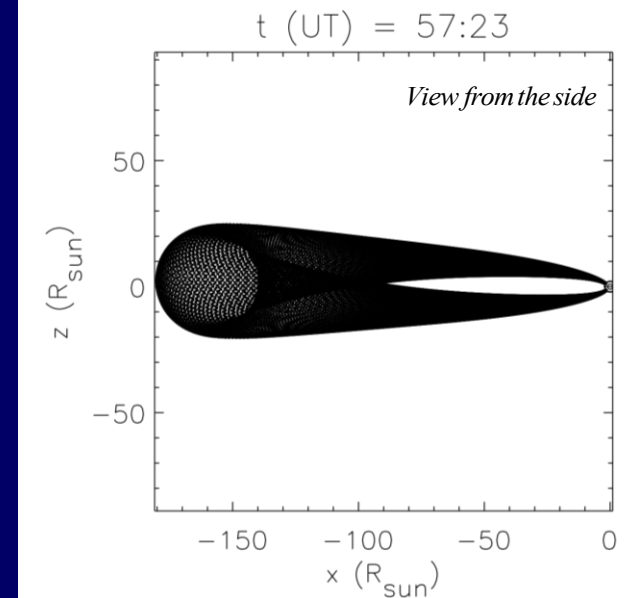
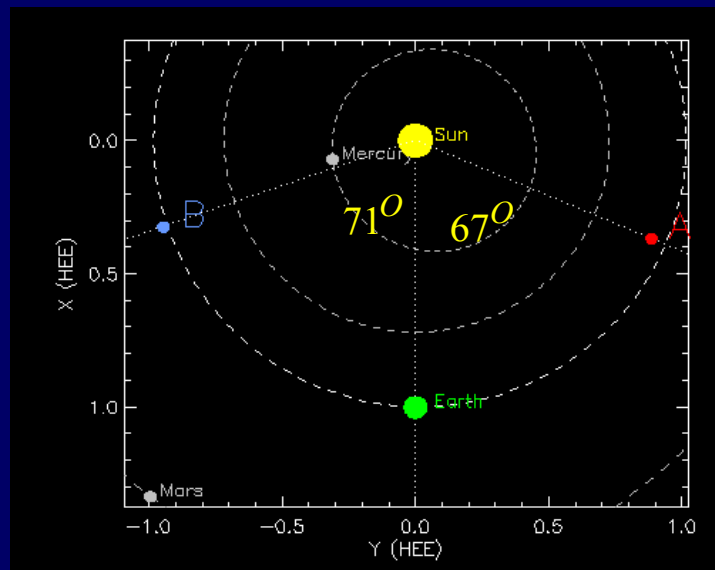
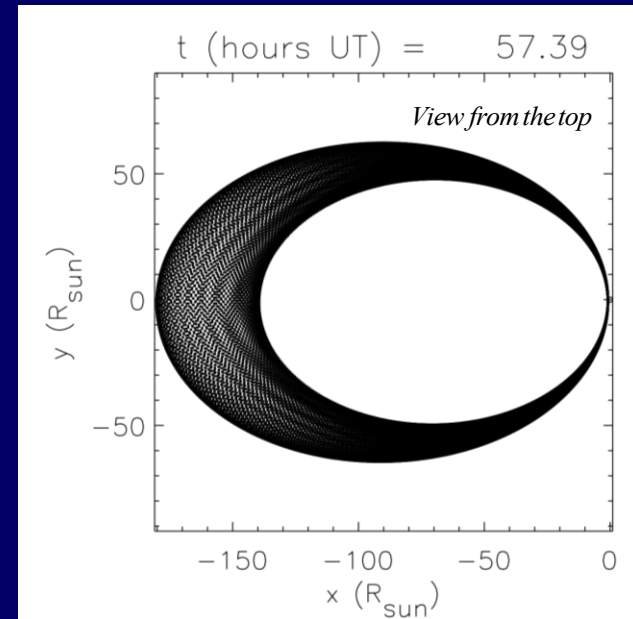
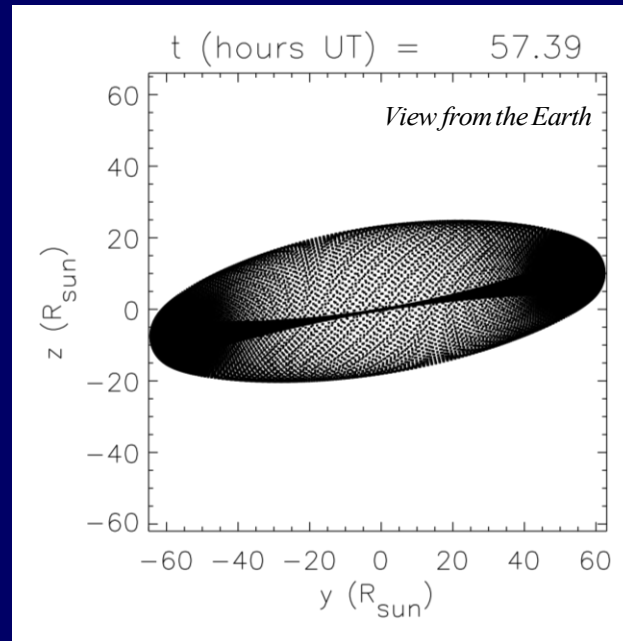


Stereo A , COR 2



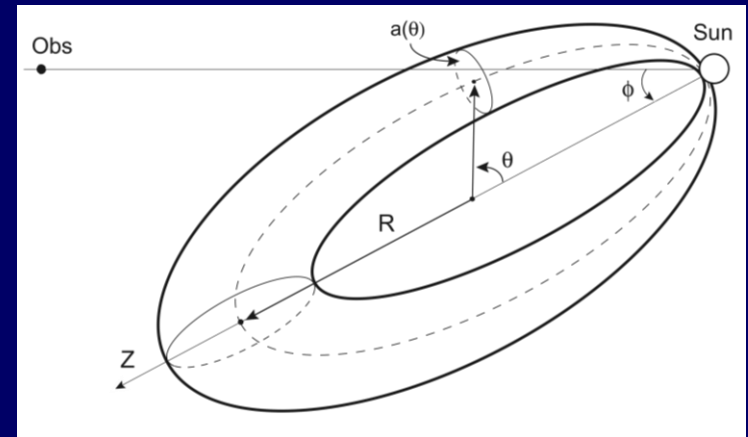
Stereo A , COR 1

# SYNTHETIC CORONAGRAPH IMAGES OF CME AT 1AU



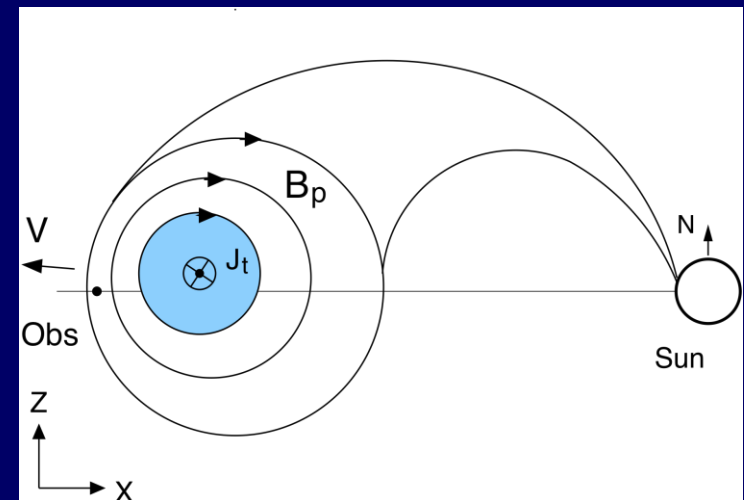
# MAGNETIC FIELD GEOMETRY IN 3D

$$B_p(r|t) = \begin{cases} 3B_{pa} \left( 1 - \frac{r^2}{a^2(t)} + \frac{r^4}{3a^4(t)} \right), & r \leq a(t), \\ 3B_{pa} \frac{r}{a(t)}, & r > a(t), \end{cases}$$

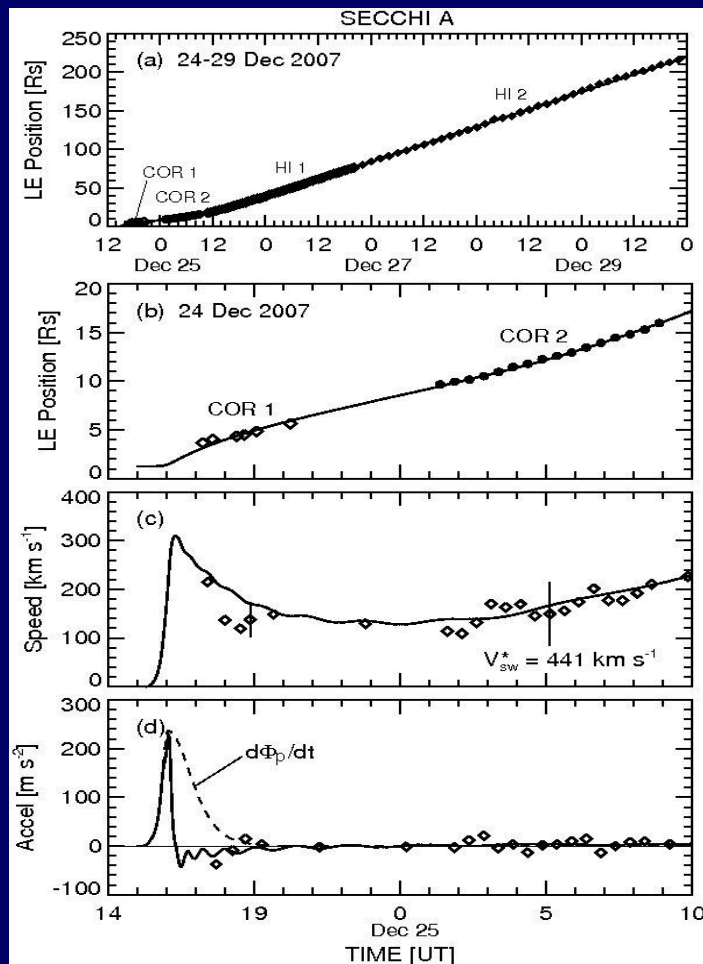


$$B_t = \begin{cases} 3B_t \left( 1 - 2\frac{r^2}{a(t)^2} + \frac{r^4}{a(t)^4} \right), & r \leq a(t) \\ 0, & r > a(t) \end{cases}$$

$a(t)$  is given by the equation of motion.

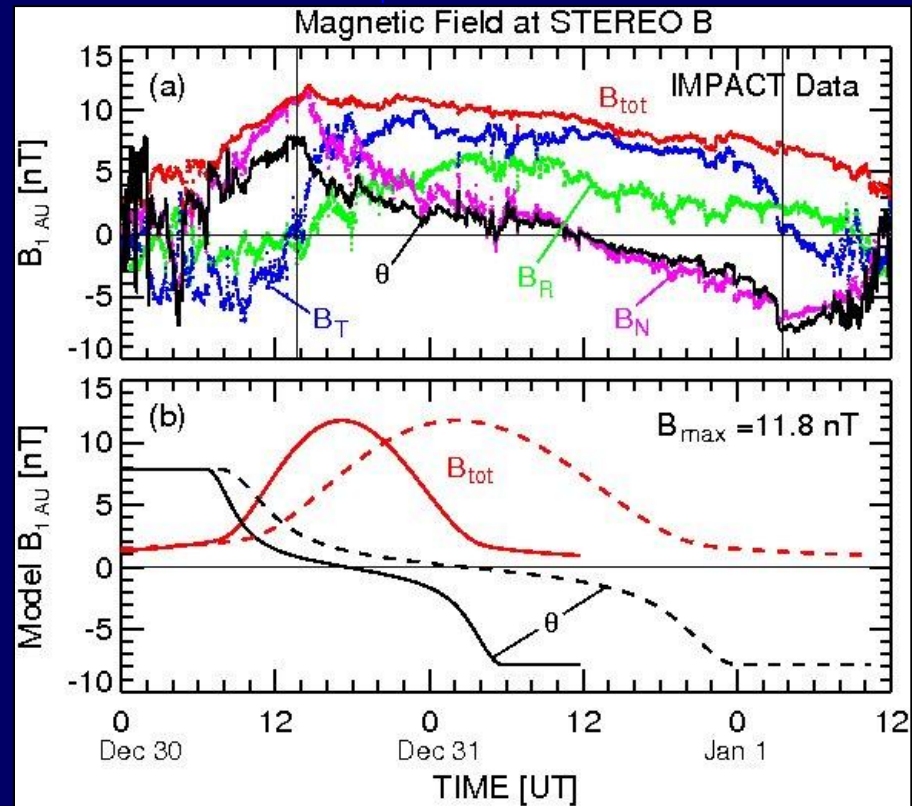


# EVOLUTION OF B FIELD AT 1AU



Calculated  $B$  field and plasma data are consistent with STEREO data at 1 AU

## Interplanetary "Magnetic Cloud"



Angle of intersection with flux-rope axis  
 — 90 deg    - - - 55 deg

Physically, MC (*Burlaga*) = current channel

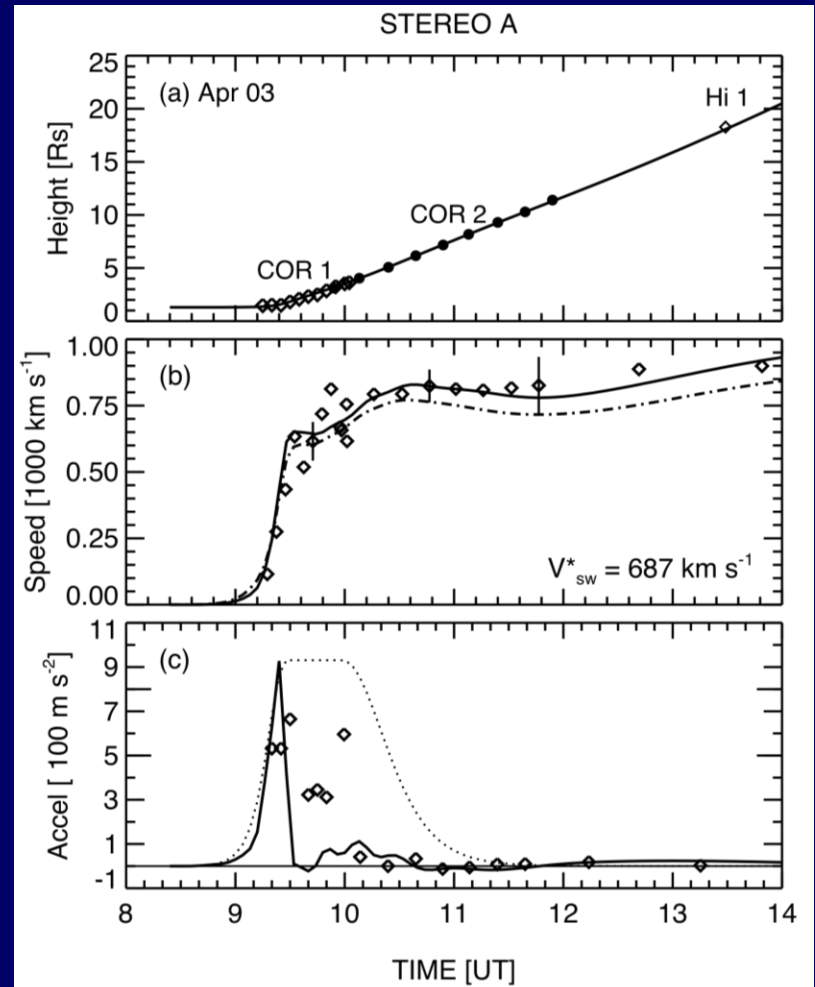
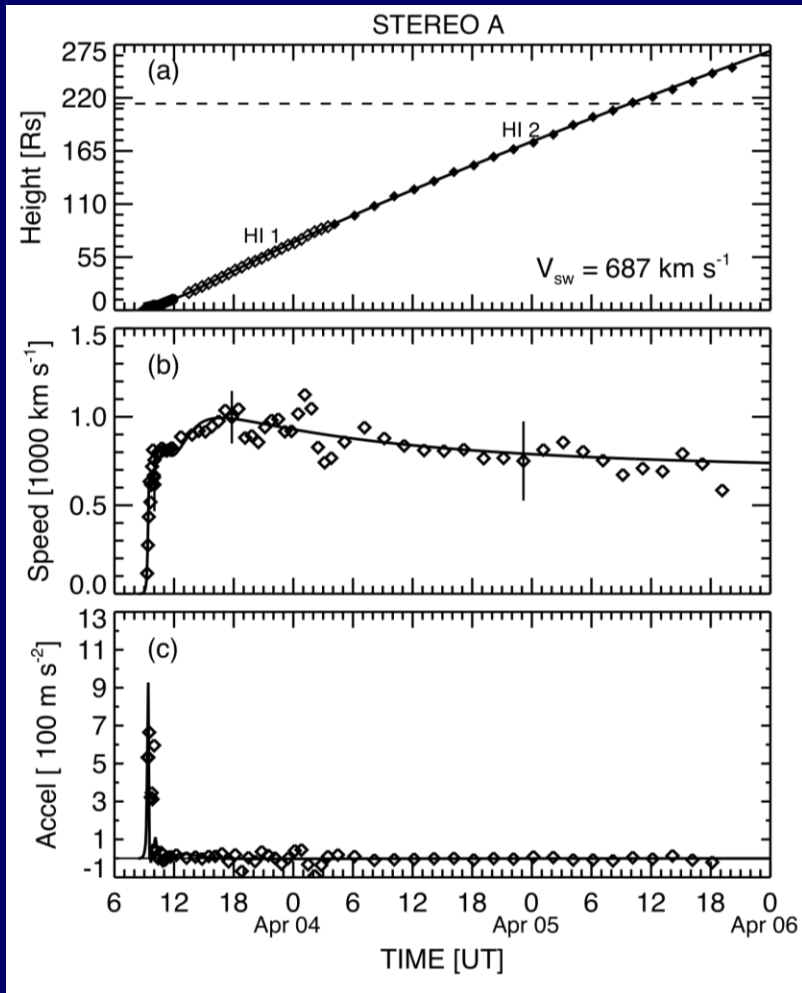
# MAGNETIC FIELD IN 1 AU AND $S_f$

Output quantities of minimum –D solutions

Best-Fit Initial Flux Rope parameters for 2007 Dec 24 Event

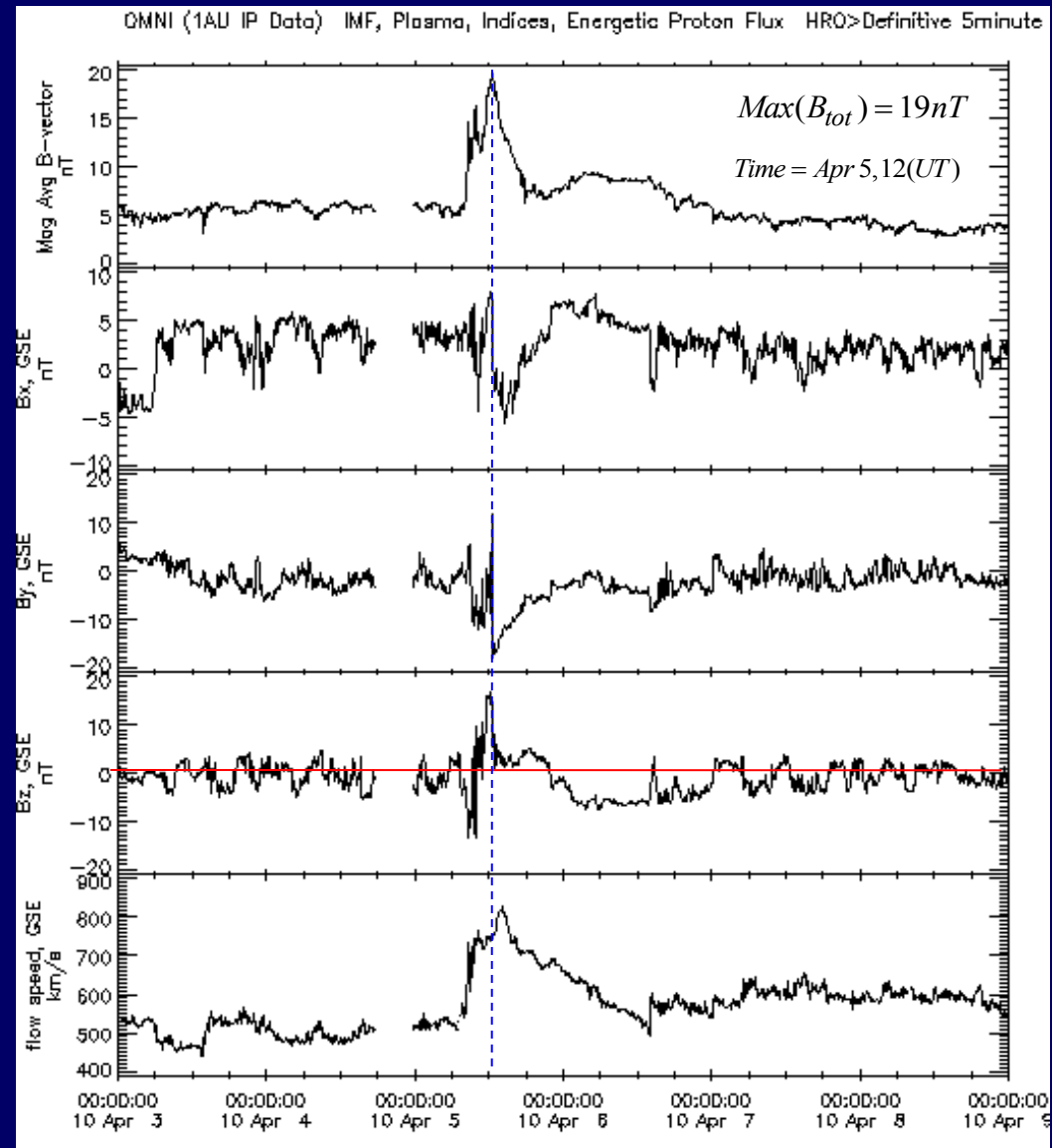
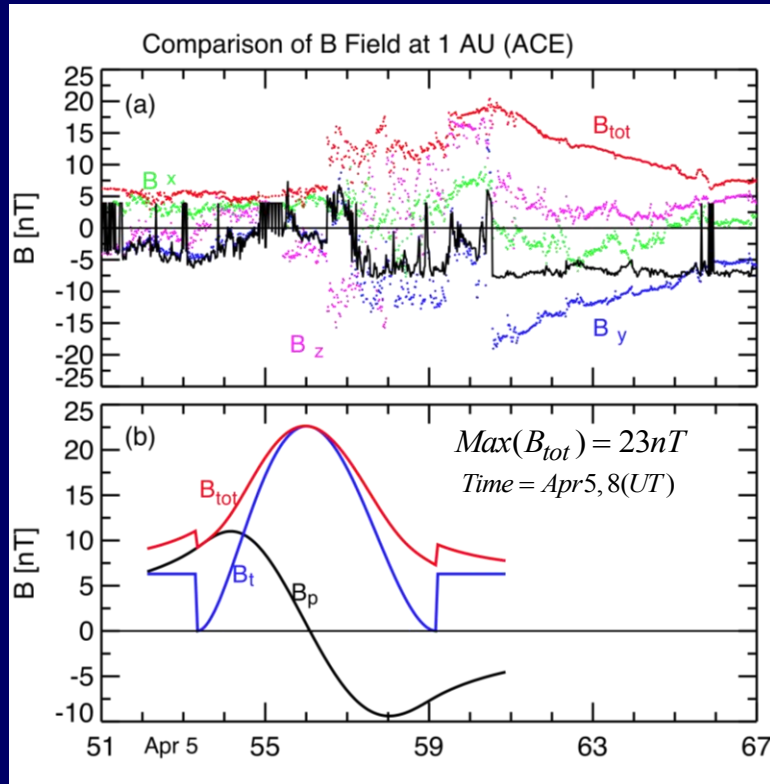
<b>G</b>	<b><math>S_f</math></b>	<b><math>Z_0</math></b>	<b><math>B_{c0}</math></b>	<b><math>B_{total}</math></b>	<b><math>V_{sw}</math></b>	<b>Arriving Time 1AU</b>	<b>Arriving Time 1AU</b>
	$[10^5 \text{ km}]$	$[10^5 \text{ km}]$	$[G]$	$[nT]$	$[km \text{ s}^{-1}]$	$[hours]$	$[Date / hours]$
1.75	1.0	0.4	-1.0	14.20	400	149	Dec 30, 7UT
0.96	1.2	0.6	-1.0	13.80	400	151.5	Dec 30, 9UT
0.35	1.8	0.8	-1.0	13.40	450	156.5	Dec 30, 12.5UT
0.42	2.0	0.8	-1.0	13.20	450	159	Dec 30, 15UT
0.75	2.5	1.2	-1.0	13.10	500	160	Dec 30, 18UT
1.76	3.0	1.8	-1.0	18.80	500	164.5	Dec 30, 22.5UT

# THEORY FIT TO CME TRAJECTORY

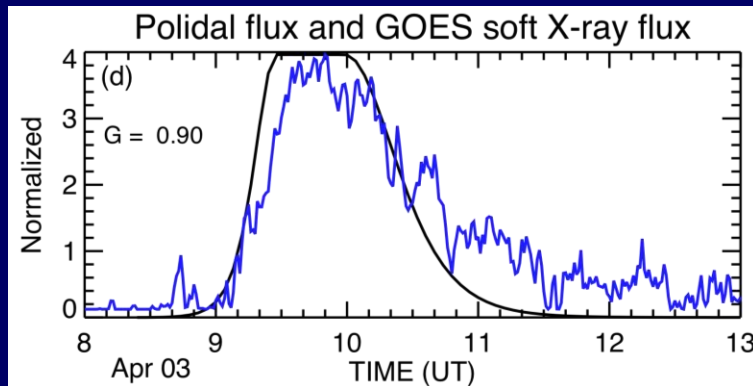
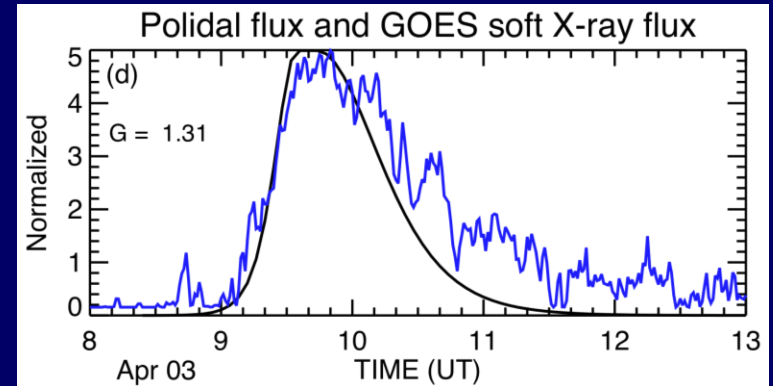
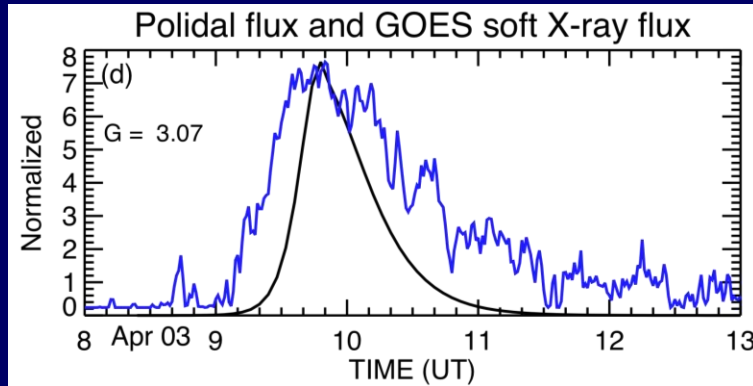


$Sf = 1.6e+05$   $Z0 = 6.0e+04$   $G = 0.90$   $tshft = 8.40$

# EVOLUTION OF B FIELD AT 1AU



# Poloidal Flux and GOES soft X-ray flux



$G$	$\Phi_{p0}$	$(d\Phi_p / dt)$	$(\Delta U_p)_{tot}$	$B(1AU)$	$T(1AU)$
	[Mx]	[Mx / sec]	[erg]	[nT]	[UT]
3.07	$4.55 \cdot 10^{20}$	$7.29 \cdot 10^{18}$	$8 \cdot 10^{31}$	23	56
1.15	$4.55 \cdot 10^{20}$	$4.99 \cdot 10^{18}$	$8 \cdot 10^{31}$	23	56
0.89	$4.55 \cdot 10^{20}$	$3.96 \cdot 10^{18}$	$8 \cdot 10^{31}$	23	56

# SUMMARY

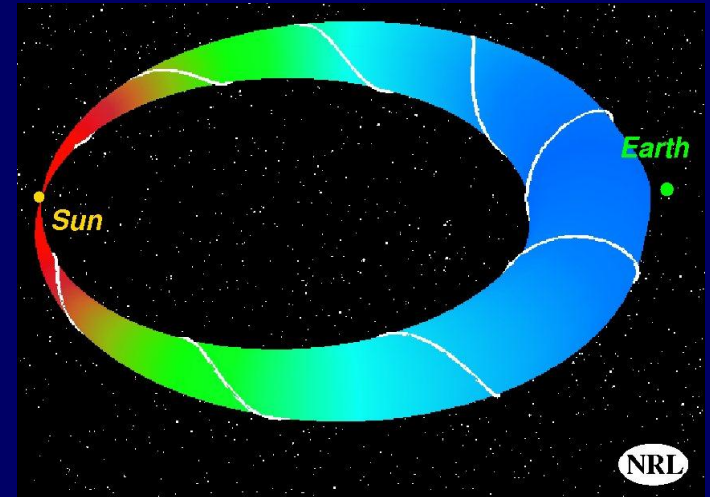
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- I have studied CME propagation using STEREO data and the flux rope model
  - Comparison of model and data shown very good agreement
- The essential ingredients of the model are:
  - (1) The CME is a magnetic flux rope with fixed footpoints in the photosphere;
  - (2) The initial equilibrium structure is set into motion by injection of the poloidal;
  - (3) The “hoop force” ( $\mathbf{J} \times \mathbf{B}$ ) acting on the flux rope provides the acceleration;
  - (4) the momentum of the erupting flux rope is coupled to the ambient coronal plasma by drag
  - (5) the hoop force dominates in the inner corona but the drag force competes with the hoop force, resulting in both acceleration and deceleration.
- Magnetic field and arrival time of the CME at 1AU are not sensitive to the Flux injection profile provided that the injected poloidal magnetic energy is unchanged
- Compared the predicted magnetic field at 1 AU with IMPACT/PLASTIC data on STEREO finding good agreement

# CALCULATED MAGNETIC FIELD

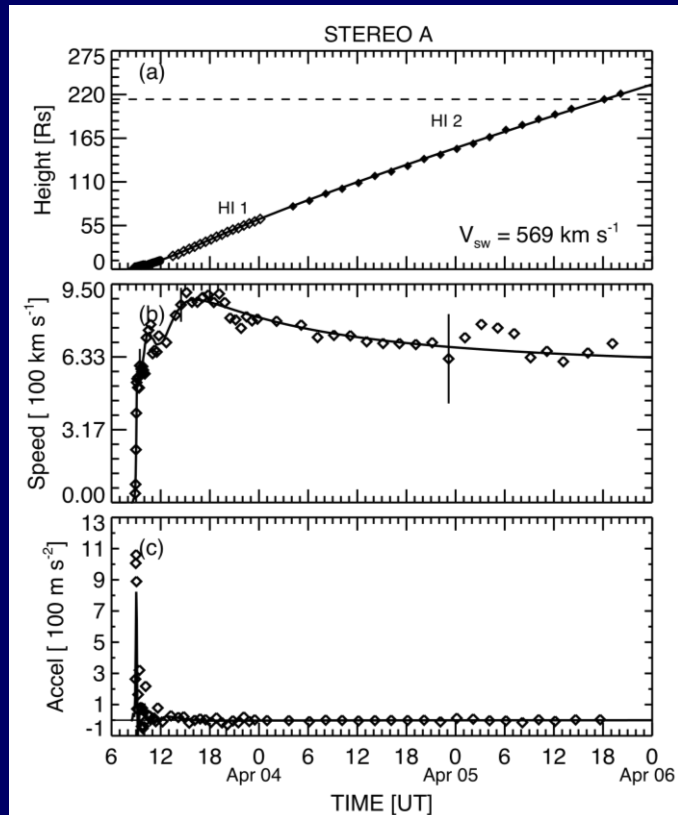
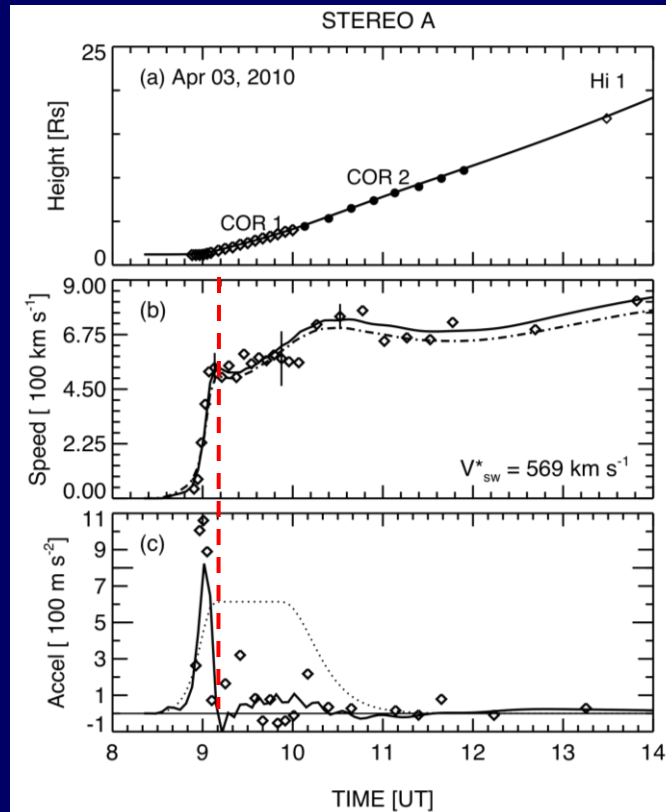
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$$B_t = \begin{cases} 3B_t \left( 1 - 2\frac{r^2}{a(t)^2} + \frac{r^4}{a(t)^4} \right), & r \leq a(t) \\ 0, & r > a(t) \end{cases}$$



$a(t)$  is given by the equation of motion.

# THEORY FIT TO CME TRAJECTORY



$$Sf = 1.0e+05 \quad Z0 = 3.1e+04 \quad G = 1.35 \quad tsft = 8.35$$

Two phases of acceleration: the **main** and **residual** acceleration phases

The main phase: Lorentz force ( $\mathbf{J} \times \mathbf{B}$ ) dominates

The residual phase: All forces are comparable, all decreasing with height

A general property: verified in ~30 CME and EP events (also *Zhang et al. 2001*)